Paper 4-Fundamentals of Business Mathematics and Statistics

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<u>SET - I</u>

Paper 4-Fundamentals of Business Mathematics and Statistics

The figures in the margin on the right side indicate full marks. This question paper has two sections. Both the sections are to be answered subject to instructions given against each.

Full Marks: 100

Time allowed: 3 Hours

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Section – A (Business Mathematics) I. (a) Choose the correct answer [9 × 2 = 18] 1. The number to be added to each term of the ratio 3 : 7 to make it 1 : 2 is (a) 2 (b) 1 (c) 3 (d) None of these 2. At what rate p.a. S.I. will a sum of money double itself in 25 years? (a) 4% (b) 3% (c) 5% (d) 6% 3. If A : B = 3 : 4 & B : C = 2 : 5, then A : B : C (a) 3:4:5 (b) 3 : 4 : 10 (c) 4 : 3 : 10 (d) 3 : 4 : 8 4. A.M. of two integral numbers exceeds their G.M. by 2 and the ratio of the numbers is 1 : 4. Find the numbers. (a) 5, 20 (b) 1, 4 (c) 2, 8 (d) 4, 16 5. Set of even positive integers less than equal to 6 by selector method. (b) {x/x=6} (c) {x/x≤6} (d) None (a) {x/x<6} 6. The value of $\log_{\sqrt{2}}^{32}$ is (b) 5 (a) 5/2 (c) 10 (d) 1/10 7. If ${}^{n}p_{3} = 120$ then n = _____ (a) 8 (b) 4 (d) None of these (c) 6 8. If ${}^{r}c_{12} = {}^{r}c_{8}$ find ${}^{22}c_{r}$ (a) 213 (b) 321 (d) None of these (c) 231 9. If $3x^2 + 6x + 3 = 0$, then roots of the equation are (a) (3, 3) (b) (-1, -1) (c) (2, 4) (d) (4, 1) (b) State whether the following statements are true or false (6×1=6)

(1) If 15% of x = 20% of y then x : y = 4 : 3

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(2) If the terms -1 + 2x, 5, 5+x are is an A.P. then x is 4	()
(3) The statement "Equivalent sets are always equal" is true or false	()
(4) The logarithm of one to any base is zero	()
(5) ⁿ c ₀ = 1 is true or false	()
(6) The degree of the equation $3x^5 + xyz^2 + y^3$ is 3	()

II. Answer any four questions. Each question carries 4 marks [4 × 4 = 16]

1. If
$$\frac{x}{b+c} = \frac{y}{c+a} + \frac{z}{a+b}$$
 then show that $(b-c)(x-a) = (c-a)(y-b) = (a-b)(z-c) = 0$.

- 2. Which is better investment 3% per year compounded monthly (or) 3.2% per simple interest (given that (1.0025)¹² = 1.0304)
- 3. Insert 4 arithmetic means between 4 and 324.

4. Prove that
$$\frac{\log\sqrt{27} + \log 8 + \log\sqrt{100}}{\log 14400} = \frac{3}{4}$$

- 5. Prove that CALCUTTA is twice of AMERICA in respect of number of arrangements of letters.
- 6. If the roots of the equation $ax^2 + bx + c = 0$ in the ratio 2 : 3, then show that $6b^2 = 25ca$.

Section - B

 $[12 \times 2 = 24]$

III. (a) Choose the correct answer

1.				and their covariance is 24. If series will be (d) 5.54
2.	Which of the follo (a) Mean	wing measures of ave (b) Median	rages divide the obser (c) Mode	vation into four equal parts (d) Quartile
3.	A variable which (a) Continuous	can assume any value (b) Discrete Value	e between two given v (c) Random	alue is called (d) None
4.	Class mark is (a) A midpoint of (c) Lower class	class interval	(b) Upper point of clo (d) None	ass interval
5.	For the observation (a) 10	ons 6, 4, 6, 5, 10, 4, 8 ra (b) 9	nge is (c) 8	(d) None

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6	(a) Aver (b) Aver (c) Aver	Harmonic mean is used for calculating (a) Average Growth Rate of Variables (b) Average speed of journey (c) Average rate of increase in net worth of a company (d) All the above 1 to 3					
7.	$x = \frac{31}{6} - \frac{y}{6}$	$\frac{7}{5}$ is the regress	ion equation	of			
	• •	x (b) x		(c) both	(d) None		
8	. Two regr (a) r = 0	ession lines co (b) r		(c) r = +1 or -	1 (d) None		
9	. The mod (a) 5.1	e for the series (b) {		, 9, 5, 8, 6 is (c) 6	(d) 8		
1	(a) Degr	deviation is u ee of variation t of extremes	or uniformity i		(b) Mode value (d) All the three		
1	1. If an unb (a) 0.25	iased coin is to (b) (ne probability of a (c) 0.75	btaining at least one (d) 1.00	e tail is	
1:	2. The dice (a) 1			obability that the o according as b >	event the difference 0 or b < 0 (d)	of nos. None of these	
(b) S	tate whethe	er the following	ı statements a	re true or false		(12×1=12)	
(1	(1) Horizontal base diagram is used for qualitative data (
(2	2) Median i	is a mathemat	ical average			()	
(3	(3) Co-efficient of variation = $\frac{\text{Co-efficient of variation}}{\text{Mean}} \times 100$						
(4	4) Range is	the value of d	ifference betw	veen mode and n	nedian	()	
(!	⁵⁾ If a coin	is tossed, then	probability of	getting two head	s is zero	()	
(4	6) If an un exclusive		tossed once	e, then the two e	events head and ta	il are mutually ()	
(7	7) 10 th perc	entile is equal	to 9 th Decile			()	
(8	8) Mean de	eviation can ne	ever be negati	ive		()	
(9	9) The value of correlation co-efficient lies between 0 & 1					()	

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(10) Bivariate data are the data collected for two variables	()
(11) When all value s are equal, then standard deviation would be zero	()
(12) As the sample size increase, range tends to decrease	()
IV. Answer any four questions. Each question carries 6 marks	[4 × 6 = 24]

- (1) Prove that for any two positive real quantities $AM \ge GM \ge HM$.
- (2) Find the median and mode of the following grouped frequency distribution:

Salaries (in ₹) per hours		10-14	15-19	20-24	25-29	Total
No. of Persons	10	20	30	25	15	100

- (3) The marks obtained by 6 students were 24, 12, 16, 11, 40, 42. Find the range. If the highest mark is omitted, find the percentage change in the range.
- (4) Calculate Karl Pearson's coefficient of correlation between variables X and Y using the following data:

Х	20	40	30	25	10	5	10	15	30	20
Y	10	25	40	15	20	40	28	22	15	5

(5) The data about the sales and advertisement expenditure of firm are given below:

Commodity	Sales (₹ In crores)	Advertisement Expenditure (₹ In crores)			
Mean	40	6			
Standard deviation	10	1.5			
Coefficient of correlation	0.9				

- (i) Estimate the likely sales for a proposed advertisement expenditure of $\stackrel{?}{\stackrel{?}{\stackrel{?}{\rightarrow}}$ 10 crores.
- (ii) What should be the advertisement expenditure if the firm proposes a sales target of ₹ 60 crores?
- (6) What is the change that a leap year, selected at random will contain 53 Sundays?